



# What a (communication) network is about

In the old days: a number of workstations over a LAN

## Today

### Collaborative Computing Systems

- Military command and control
- Online strategy games
- Massive computation

### Distributed Real-time Systems

- Process Control
- Navigation systems, Airline Traffic Monitoring (ATM)

### Mobile Ad hoc Networks

Rescue Operations, emergency operations, robotics

### Wireless Sensor Networks

Habitat monitoring, intelligent farming

### Social Networks

### Grid and Cloud computing

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# Lack of cooperativeness in large networks

Large networks (e.g., Internet) are built and controlled by diverse and competitive entities:

- Entities own different components of the network and hold private information
- Entities are selfish and have personal preferences

⇒ The classic **network optimization** field of research (where selfishness is not considered) does not fit properly!

# Three main ingredients in the course: Networks + Algorithms + Game Theory

**Non-cooperative Network (NCN):** Broadly speaking, we refer to it as a set of autonomous (i.e., **non-cooperative**) computational devices (say, processors or agents) performing multiple operations/tasks simultaneously, and which influence reciprocally either by **taking actions** or by **exchanging messages** (using an underlying wired/wireless communication infrastructure)

We will be concerned with the **computational** and **game-theoretic aspects** of a NCN. We will analyze a NCN by assuming that each agent chooses **strategically** and **non-cooperatively** how to behave, by aiming to maximize his personal benefit. Our topic is a subfield of the larger emerging **Algorithmic Game-Theory (AGT)** field.

# Course structure

FIRST PART: Strategic equilibria theory in NCN

1. Nash equilibria
2. Selfish routing
3. Network Design games
4. Network Creation games

SECOND PART: Implementation theory in NCN

1. Algorithmic mechanism design (AMD)
2. AMD for some basic graph optimization problems

**Mid-term Written Examination** (at the end of the first part of the program): 10 multiple-choice tests, plus an open-answer question

**Final Oral Examination:** this will be concerned with either the whole program or just the second part of it, depending on the outcome of the mid-term exam.

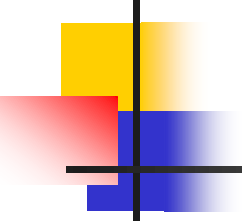
There will be fixed a total of 6 dates, namely:

- 3 in January-February
- 2 in June-July
- 1 in September

For those enrolled in the NEDAS curriculum, there will be a single final grade as a result of the grades obtained in this course and in the 'Social Networks' course; the corresponding exams can be done separately, but they must be sustained within the same calendar year

# Suggested readings

- *Algorithmic Game Theory*, Edited by Noam Nisan, Tim Roughgarden, Eva Tardos, and Vijay V. Vazirani, Cambridge University Press.
- Blog by Noam Nisan  
<http://agtb.wordpress.com/>



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**Algorithmic Issues in  
Strategic (Non-cooperative)  
Distributed Systems  
(Networks)**





# Two Research Traditions

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- Theory of Algorithms: computational issues
  - What can be feasibly computed?
  - How long does it take to compute a solution?
  - Which is the quality of a computed solution?
  - Centralized or distributed computational models
- Game Theory: interaction between self-interested individuals
  - What is the outcome of the interaction?
  - Which social goals are compatible with selfishness?



# Different Assumptions

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- Theory of Algorithms (in distributed systems):
  - Processors are *obedient, faulty (i.e., crash), adversarial (i.e., Byzantine)*, or they compete without being strategic (*e.g., concurrent systems*)
  - *Large* systems, *limited* computational resources
- Game Theory:
  - Players are *strategic* (selfish)
  - *Small* systems, *unlimited* computational resources



# The Internet World

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- Users often selfish
    - Have their own individual goals
    - Own network components
  - Internet scale
    - Massive systems
    - Limited **communication/computational** resources
- ⇒ *Both **strategic** and **computational** issues!*



# Fundamental question

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- How the **computational aspects** of a **strategic** distributed system should be addressed?

*Algorithmic  
Game Theory* = *Theory of  
Algorithms* + *Game  
Theory*



# Basics of Game Theory

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- A **game** consists of:
  - A set of **players** (or **agents**)
  - A specification of the **information** available to each player
  - A set of rules of encounter: **Who** should act **when**, and **what** are the possible actions (**strategies**)
  - A specification of **payoffs** for each possible **outcome** (combination of strategies) of the game
- **Game Theory** attempts to predict the **final outcomes** (or **solutions**) of the game by taking into account the individual behavior of the players



# Solution concept

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How do we establish that an outcome is a **solution**? Among the possible outcomes of a game, those enjoying the following property play a fundamental role:

- **Equilibrium solution**: strategy combination in which players are **not willing** to change their state. But this is quite informal: what does it rationally mean that a player does not want to change his state? In the **Homo Economicus** model, this makes sense when he has selected a strategy that maximizes his *individual wealth*, knowing that other players are also doing the same.



# Roadmap

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- We will focus on two prominent types of equilibria: Nash Equilibria (NE) and Dominant Strategy Equilibria (DSE)
- Computational Aspects of Nash Equilibria
  - Can a NE be feasibly computed, once it exists?
  - What about the "quality" of a NE?
  - **Case study:** Network Flow Games (i.e., selfish routing in Internet), Network Design Games, Network Creation Games
- (Algorithmic) Mechanism Design
  - Which social goals can be (efficiently) implemented in a strategic distributed system?
  - Strategy-proof mechanisms in DSE: Vickrey-Clarke-Groves (VCG)-mechanisms and one-parameter mechanisms
  - **Case study:** Shortest Path, Minimum Spanning Tree, Single-source Shortest-path Tree, Single-Minded Combinatorial Auctions